

Each graph below represents a value semigroup obtained from the coordinate ring of an SL_r free group character variety. The rank of the associated free group can be recovered as half the number of vertices of the graph plus one, or equivalently as the first Betti number. As this rank grows, many different semigroups provide a combinatorial picture of the same coordinate ring.